

Creating Diversity in 5G via Beam Pattern Jittering

Real Time Signal Processing Challenges for Massive MIMO SDR

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Goals:

- Enhance capacity (*numbers of users or throughput*),
- Increase QoS (probability-of-error performance),
- Reduced Cost

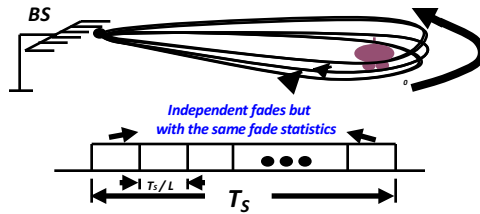
A merger of Directionality AND Transmit Diversity

HOW? Adaptive Antenna Arrays at the BS:

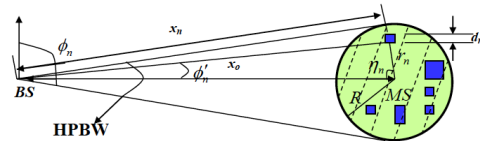
- (1) **Proper Phase shifts** → Directionality (Spatial Multiplexing)
 - Higher Capacity
- (2) **Moving beam pattern** → Transmit Diversity (Induced Time Diversity)
 - Improved probability-of-error performance
- (3) **Low Cost:** Complexity remains at the BS, Low MS Complexity

Examples of Beam Pattern Movement:

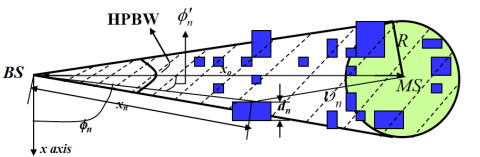
Beam Pattern Oscillation; Beam Pattern Beating



Circular Channel Model for High Altitude BS



Semi-Elliptical Channel Model for Low Altitude BS

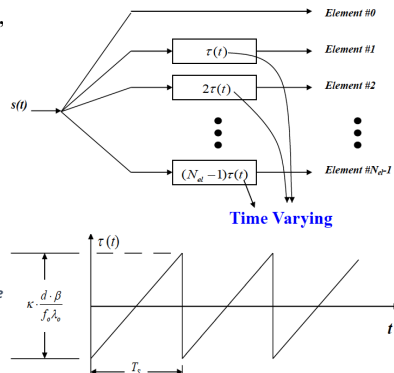


$$h(t, \tau) = \sum_{n=1}^{N(t)} \alpha_n(t) \cdot e^{j\phi_n(t, \phi_n)} \cdot \delta(\tau - \tau_n)$$

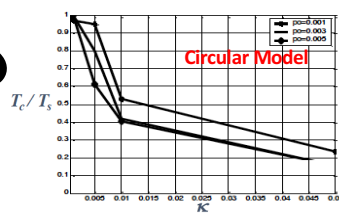
1. HPBW ∈ [0.1rad, 0.5 rad], 6°, 28°
 2. P_o ∈ [1, 5] scatterers / 1000m²

The control parameter $\kappa \in [0.0005, 0.05]$:
 Antenna pattern movement between 0.05% to 5% of its HPBW.

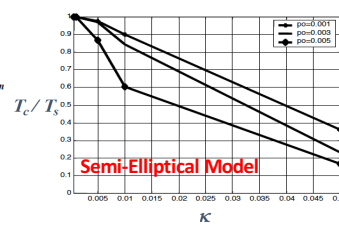
S. A. Zekavat, and C. R. Nassar, "Transmit diversity via oscillating beam pattern adaptive antennas: An evaluation using geometric-based stochastic circular-scenario channel modeling," *IEEE Transactions on Wireless Communications*, vol. 4, no. 3, pp. 1134-1141, July 2004.
 S. A. Zekavat, C. R. Nassar and S. Shattil, "Merging multi-carrier CDMA and oscillating-beam smart antenna arrays: Exploiting directionality, transmit diversity and frequency diversity," *IEEE Transactions on Communications*, vol. 52, no. 1, pp. 110 - 119, Jan. 2004.
 S. A. Zekavat, C. R. Nassar, "Power-aimuth-spectrum modeling for antenna array systems: A geometric-based approach," *IEEE Transactions on Antennas and Propagation*, vol. 51, no. 12, pp. 3292 - 3294, Dec. 2003.
 S. A. Zekavat, and C. R. Nassar, "Smart antenna arrays with oscillating beam patterns: Characterization of transmit diversity using semi-elliptical-coverage geometric-based stochastic channel modeling," *IEEE Transactions on Communications*, vol. 50, no. 10, pp. 1549-1556, Oct. 2002.



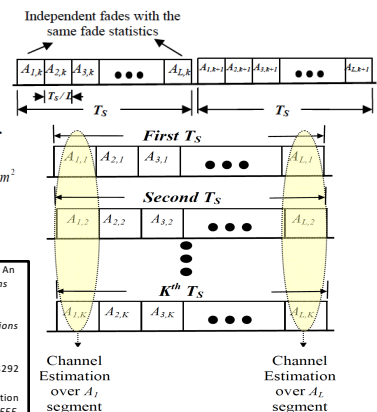
BS-MS distance=500 m, HPBW=28 deg.



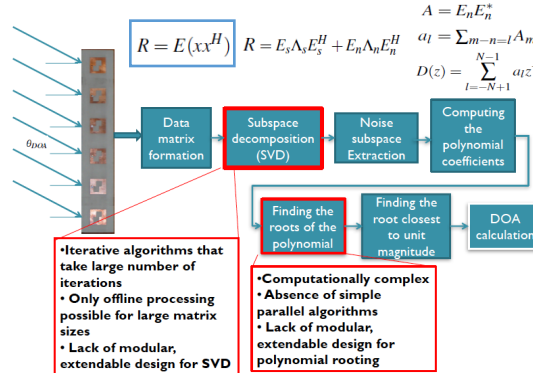
BS-MS distance=500 m, HPBW=28 deg.



$A_{i,k}$: The j^{th} time segment within k^{th} symbol time duration. In these segments independent fades are experienced due to BPS.



Real-time implementation of root-MUSIC

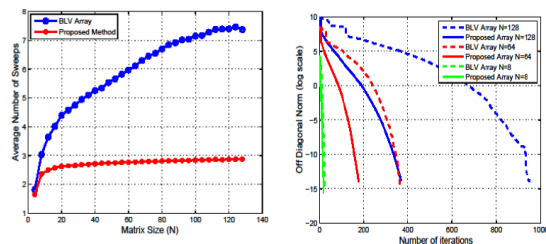
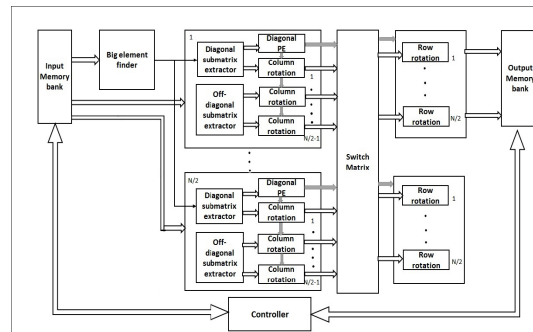


Brent-Luk-Van (BLV) SVD:

Special purpose CORDIC algorithm → computation reduction → FPGA Implementation
 Not Suitable for Large Matrices

Proposed SVD:

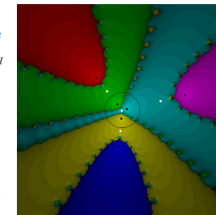
- In each iteration target the biggest element and few other big elements
- These set of four big elements need to be row and column exclusive
- No exchange of data between iterations is required.
- We term this as "dynamic ordering" unlike Jacobi methods which follow predefined "fixed ordering"



Improvement more Evident as Matrix Size Increases;

M. Athi, S. A. Zekavat, and A. A. Struthers, "Real Time Signal Processing of Massive Sensor Arrays via a Novel Fast Converging SVD Algorithm: Latency, Throughput and Resource Analysis," *IEEE Sensors Journal*, vol. 16, no. 08, pp. 2519-2526, 2016.

Real-time root-MUSIC DOA estimation via Parallel Polynomial Rooting



Newton map:

$$N_p: \mathbb{C} \rightarrow \mathbb{C}, z \rightarrow z - \frac{p'(z)}{p(z)}$$

Critical points:

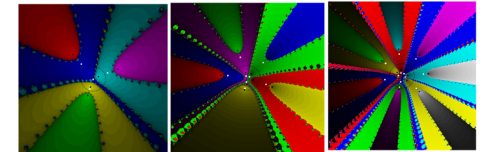
$$N_p'(z) = \frac{p'(z)p''(z)}{p'(z)^2} = 0$$

Properties:

1. Symmetry of Roots across Unit Circle;
2. Access to Infinity=M-2

M Poly. Degree

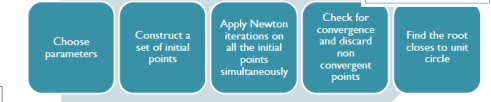
Newton Map of Root-MUSIC Polynomial in Various Antenna Array Conditions



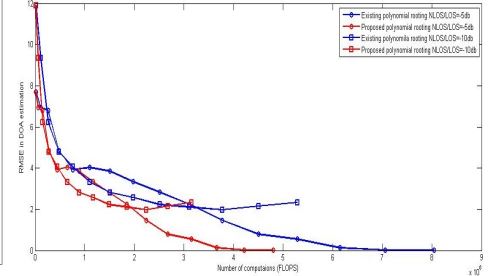
4 antenna elements, degree=6
 6 antenna elements, degree=10
 8 antenna elements, degree=14

Tolerance, Iterations

$$\text{Choose } \epsilon, N_i \quad \hat{z}_k = 1 + \epsilon^{1/k} \omega^k, \quad k = 1, \dots, N_i \quad z_j = z(j-1) - \frac{p'(z(j-1))}{p'(z(j-1))}$$



Rician channel with one non-line of sight (NLOS) path



| Method | Computational Complexity | Parallel Implementation | Comments |
|---|--------------------------|---|----------------------------------|
| Eigenvalue of companion matrix using QR decomposition | $O(d^3)$ | None, QR decomposition is inherently sequential | Each QR step is $O(d^2)$ |
| Fast QR based on n^{th} root of unity | $O(d^2)$ | None, QR decomposition is inherently sequential | Each QR step is $O(d)$ |
| Roots by balanced factorization of polynomial | $O(d \log^2(d) \log B)$ | $O(\log^2(d)) \log b$ using $O(d \log^2(d))$ processors | Factorization introduces error |
| Newton's method for general polynomials | $O(d^2 \log^2(d))$ | $O(d)$ using $O(d \log^2(d))$ processors | Large set of initial points |
| Proposed method | $O(d^2)$ | $O(d)$ using $O(d)$ processors | Method specific to RM polynomial |

M. Athi, and S. A. Zekavat, "A novel parallel polynomial rooting technique for root-MUSIC" proceedings *IEEE PIMRC 2014*, Sept. 02-05 2014, Washington DC.